Regular Polygons - Central, Interior, and Exterior Angles

1. A **Regular Polygon** is ______. Several Regular Polygons are given in this module. Use these figures along with your protractor to perform the following investigations.

2. Explore the relationship of the number of sides of a regular polygon and the **Central Angles**. Fill in the following table and make a generalization about Regular N-gons.

| Name | # of Sides | Measure of a Central Angle | Sum of the Measure of the Central Angles |
|----------------------|------------|----------------------------|--|
| Equilateral Triangle | | | |
| Square | | | |
| Regular Pentagon | | | |
| Regular Hexagon | | | |
| Regular Octagon | | | |
| Regular Decagon | | | |
| Regular Dodecagon | | | |
| | | | |
| Regular N-gon | | | |

3. Write a conjecture about the Central Angles of a Regular Polygon.

4. Explore the relationship of the number of sides of a regular polygon and the **Interior Angles**. Fill in the following table and make a generalization about Regular N-gons.

| Name | # of Sides | Measure of an Interior Angle | Sum of the Measure of the Interior Angles |
|----------------------|------------|------------------------------|---|
| Equilateral Triangle | | | |
| Square | | | |
| Regular Pentagon | | | |
| Regular Hexagon | | | |
| Regular Octagon | | | |
| Regular Decagon | | | |
| Regular Dodecagon | | | |
| : | | | |
| Regular N-gon | | | |

5. Write a conjecture about **Interior Angles** of a Regular Polygon. Think about breaking apart the polygon into triangles as shown below.



Notice there are _____ triangles and the sum of the measures of the angles of each triangle is ____.

6. Explore the relationship of the number of sides of a regular polygon and the **Exterior Angles**. Fill in the following table and make a generalization about Regular N-gons.

| Name | # of Sides | Measure of an Exterior Angle | Sum of the Measure of the Exterior Angles |
|----------------------|------------|------------------------------|---|
| Equilateral Triangle | | | |
| Square | | | |
| Regular Pentagon | | | |
| Regular Hexagon | | | |
| Regular Octagon | | | |
| Regular Decagon | | | |
| Regular Dodecagon | | | |
| 1 | | | |
| Regular N-gon | | | |

7. Write a **conjecture** about Exterior Angles of a Regular Polygons.

8. **EXTENSION:** What is the area of a regular n-gon?

