

Let $g(\theta) = \frac{1}{2} \log\left(\frac{1+\theta}{1-\theta}\right)$. This is an inc. f.n. on $(-1, 1)$ since $1+\theta$ inc. on $(-1, 1)$ and $1-\theta$ dec. on $(-1, 1)$. We have

$$g^{-1}(\theta) = \frac{e^{2\theta} + 1}{e^{2\theta} - 1}.$$

(12.25) gives us that

$$\sqrt{n-3} (g(\hat{\theta}) - g(\theta)) \stackrel{\text{approx}}{\sim} N(0, 1).$$

So

$$\begin{aligned} 1-\alpha &\approx P(-z_{\alpha/2} < \sqrt{n-3} (g(\hat{\theta}) - g(\theta)) < z_{\alpha/2}) \\ &= P(g(\hat{\theta}) - \frac{z_{\alpha/2}}{\sqrt{n-3}} < g(\theta) < g(\hat{\theta}) + \frac{z_{\alpha/2}}{\sqrt{n-3}}) \\ &= P(g^{-1}(g(\hat{\theta}) - \frac{z_{\alpha/2}}{\sqrt{n-3}}) < \theta < g^{-1}(g(\hat{\theta}) + \frac{z_{\alpha/2}}{\sqrt{n-3}})). \end{aligned}$$

So to obtain an approx. c.i. for θ , get values for $g(\hat{\theta}) \pm \frac{z_{\alpha/2}}{\sqrt{n-3}}$ and apply the inv. transformation.