

# **Student Misconceptions**

Students have difficulty...

- using multiple representations to solve a problem.**
- setting up / interpreting graph/chart.**
- discerning between important and unnecessary information in problem.**
- with problem solving strategies.**

# **Student Misconceptions**

Students have difficulty...

- turning words into mathematical concepts/ideas.**
- going from concrete to abstract ideas.**
- seeing / understanding patterns.**
- turning a pattern into a rule.**

# Justification

- Problem solving or modeling based approach to algebra can improve students' attitudes towards math and increase their confidence in their mathematical abilities.
- “A modeling-based approach to college algebra.”(Virginia Commonwealth University's educational program). Aimee J. Ellington. [Academic Exchange Quarterly](#) 9.3 (Fall 2005): p131(5).
- A curriculum that focuses on algebra as more than symbolic manipulation and that considers functions, modeling, and representations as key components can provide students with a solid understanding in a fundamental area of algebra.
- “Middle grades students' algebraic understanding in a reform curriculum.” Angela S. Krebs. [School Science and Mathematics](#) 103.5 (May 2003): p233(13).

# Awesome Results....

Day	Brian	David
1	1.20	1.05
2	1.60	1.00
3	1.50	.95
4	1.40	.90
5	1.30	.85
6	1.20	.80
7	1.10	.75
8	1.00	.70
9	.90	.65
10	.80	.60
11	.70	.55
12	.60	.50
13	.50	.45
14	.40	.40
15	.30	.35
16	.20	.30
17	.10	.25
18	0	.20

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
170	160	150	140	130	120	110	100	90	80	70	60	50	40	30	20	10	0
105	100	95	90	85	80	75	70	65	60	55	50	45	40	35	30	25	20

110	105	100	95	90	85	80	75	70	65	60	55	50	45	40	35	30	25	20	15	10	5	0	
David	105	100	95	90	85	Brian	170	160	150	140	130	120	110	100	90	80	70	60	50	40	30	20	10
day	1	2	3	4	5	Day	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17
80	75	70	65	60	55	50	45	40	35	30	25	20	15	10	5	0							
6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29

Tables, tables, everywhere!

# Student samples...

"Wishing for a Puppy" Name Gabi Date 11/15/15 Pd 5

Describe any type of patterns that you see in this problem

subtracting by 5 and 10  
number is always divisible by 5

Based on the patterns that you see, create a formula that will quickly solve the problem.

$$(180 \div 5) - (110 \div 5) = 14 \text{ - day with same amount of money}$$

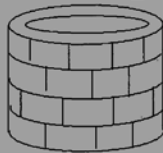
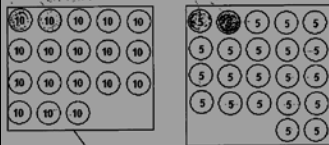
$$\begin{array}{r} 36 \\ 5 \overline{)180} \\ \underline{15} \phantom{0} \\ 30 \phantom{0} \\ \underline{30} \phantom{0} \\ 0 \phantom{0} \end{array} \quad - \quad \begin{array}{r} 22 \\ 5 \overline{)110} \\ \underline{10} \phantom{0} \\ 10 \phantom{0} \\ \underline{10} \phantom{0} \\ 0 \phantom{0} \end{array} = \boxed{14}$$

Name \_\_\_\_\_ Date \_\_\_\_\_ Pd \_\_\_\_\_

"Wishing for a Puppy"



Brian and David are two brothers that wish they could have a puppy. They decide that each morning, while walking to school, they will each wish for a puppy while throwing one of their coins into the wishing-well that is near their home. On the first morning, before school, Brian has 18 dimes at home, and David has 22 nickels. One day after school, David notices that he has more money left than Brian. How many days had passed since they started throwing coins into the well?



Brian	David
1. 180	105
2. 160	100
3. 155	95
...	...
10. 80	60
$(18-10) \times 10$	$(22-10) \times 5$
13. 50	45
...	...
15. 30	35

*Kun Ho's formulas:*  
 $(18 - 10) \times 10$   
 $(22 - 10) \times 5$

"Wishing for a Puppy" Name Jack

Describe any type of patterns that you see in this problem.

$Y = \text{Day} \times \text{money} \times M$       $22 = \text{David}$

1	170	1	105
2	160	2	100
3	150	3	95
...	...	...	...
11	180-10Y	22	110-5Y

Based on the patterns that you see, create a formula that will quickly solve the problem.

*Jack's formulas:*  $B = 1.80 - 10y$   
 $D = 1.10 - 5y$

*Gabi's formula:*  $(180/5) - (110/5) = 14$

*The day they had the same amount of money.*

money left than Brian. How many days had passed since they started well?

**BRIAN**

10	10	10	10	10
10	10	10	10	10
10	10	10	10	10
10	10	10	10	10

18 coins

**DAVID**

5	5	5	5	5
5	5	5	5	5
5	5	5	5	5
5	5	5	5	5

110

15 DAYS

# Working really hard...

well?

10	10	10	10	10
10	10	10	10	10
10	10	10	10	10
10	10	10	10	10

B

5	5	5	5	5
5	5	5	5	5
5	5	5	5	5
5	5	5	5	5

D

-10	-5
1 180	220
2 170	105
3 160	100

15 days

Later 60 50

23th 50 45

14th 40 40

15th 30 35

Way to use your Pictures, Sofia!

Based on the patterns that you see, create a formula that will quickly solve the problem.

Write computer program

start

every  $\frac{1}{2}$  sec

When

stop

Shane the Future Computer Programmer?

# Lesson Enhancement

## “Wishing for a Puppy”

Have students with quick and efficient solutions visit other groups and share their answers. This will be less frightening to those who may not want to share with the entire class.

- Students who finish early come up with more efficient ways to solve the problem.

# Lesson Enhancement

- Have a few students echo/restate other strategies used by their classmates.
- Allow students time to discuss their strategies with their group members before writing the reflection piece.





## Student Difficulties



1. IDENTIFYING AND TESTING AN ALGORITHM THAT WORKS TO SOLVE A SPECIFIC PROBLEM.
2. DIFFICULT TO MOVE FROM AN ABSTRACT THOUGHT TO CONCRETE SOLUTION.



# STAND



1. If your favorite month is \_\_\_\_\_
2. If your favorite sport is \_\_\_\_\_
3. If your favorite color is \_\_\_\_\_
4. If you are wearing socks \_\_\_\_\_
5. If your favorite season is \_\_\_\_\_
6. If the subject you plan to have an A is science \_\_\_\_\_
7. If you traveled out of the country this summer \_\_\_\_\_